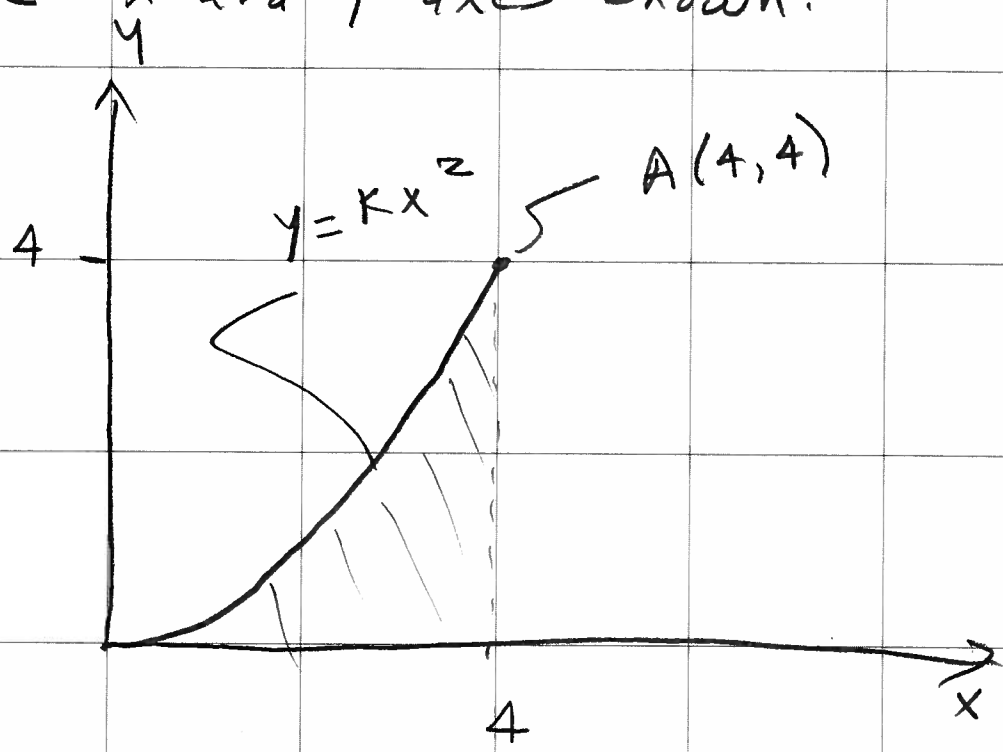


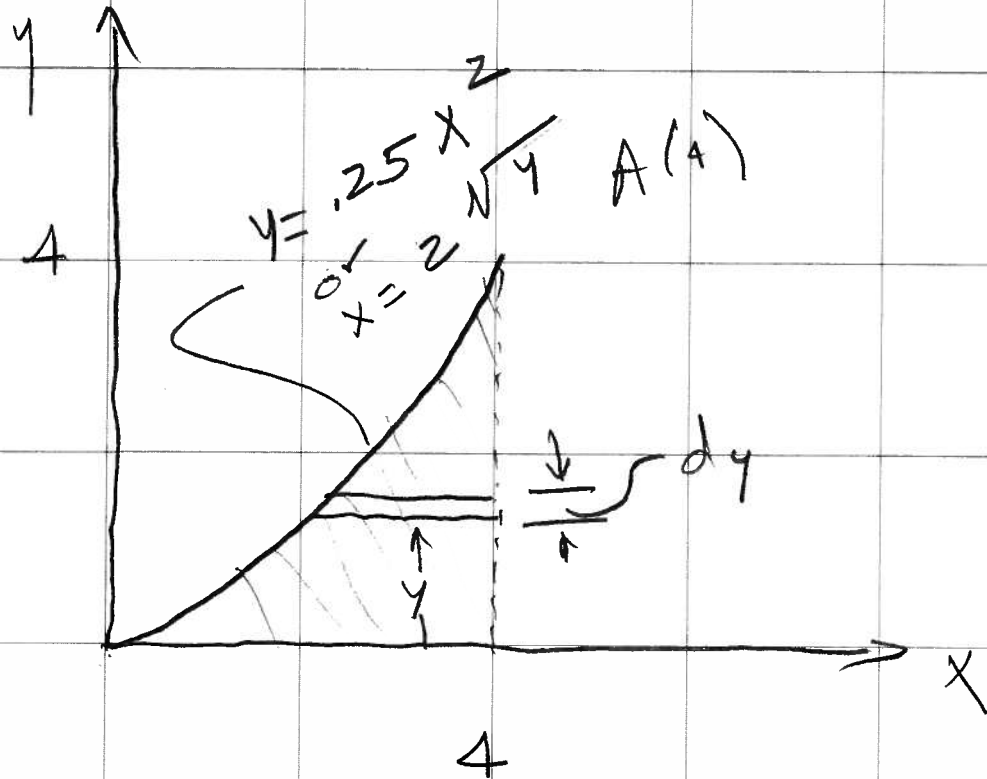
Determine the area moments of inertia about the x and y axes shown.



First determine the value of k  
Knowing that the curve goes through  
point A (4,4).

- (1)  $y = kx^2$
- (2)  $4 = k(4)^2$
- (3)  $k = \frac{1}{4} = .25$
- (4) so  $y = .25x^2$

To calculate the moment of inertia about the x-axis, choose a differential element that is parallel to the x-axis as shown



$$(5) \quad dA = (4 - x) dy$$

$$(6) \quad dA = (4 - 2\sqrt{y}) dy$$

By definition

$$(7) \quad I_x = \int y^2 dA$$

So

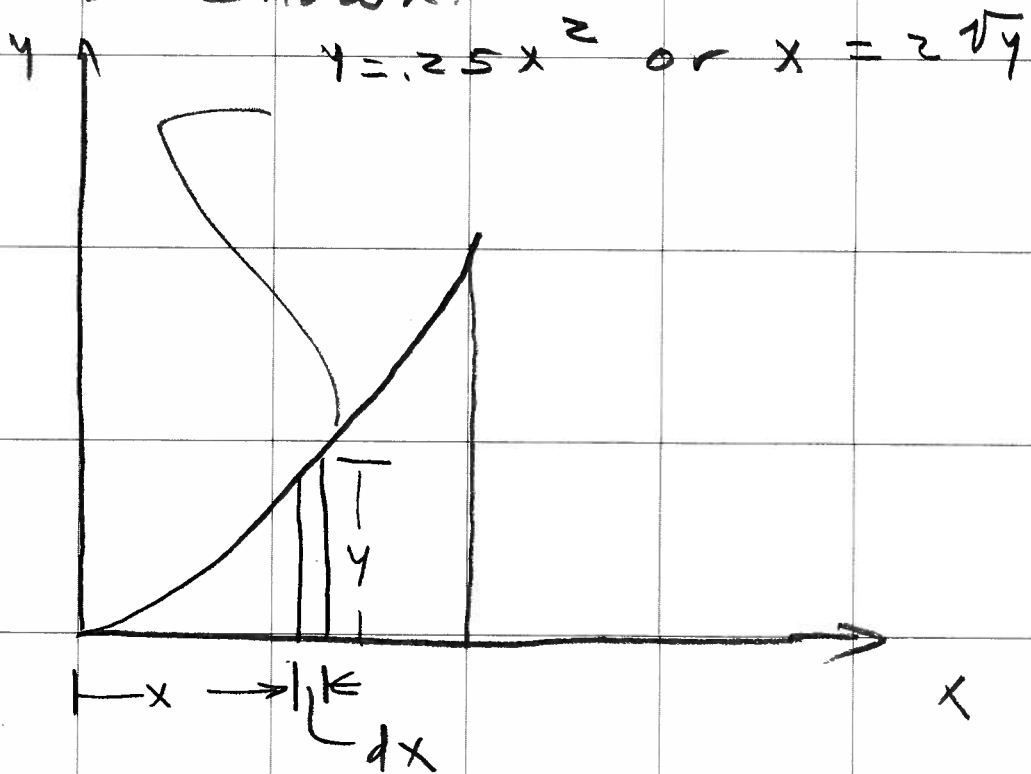
$$(8) \quad I_x = \int_0^4 y^2 (4 - 2\sqrt{y}) dy$$

$$\int (y^2 * (4 - 2 * \sqrt{y})), y, 0, 4$$

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$$(9) \quad I_x = 12.19 \quad (\text{in}^4, \text{mm}^4, \text{etc}^4)$$

To calculate the moment of inertia about the y-axis, choose a differential element that is parallel to the y-axis as shown.



In this case

$$(10) \quad dA = y \, dx$$

$$(11) \quad dA = .25x^2 \, dx$$

By definition

$$(12) \quad I_y = \int x^2 \, dA$$

So

$$(13) \quad I_y = \int_0^4 x^2 (.25x^2) \, dx$$

$$(14) \quad I_y = \int_0^4 .25x^4 \, dx$$

$$\int (.25 * x^4, x, 0, 4)$$

$$(15) \quad I_y = 5/2 \quad (\text{in}^4, \text{mm}^4, \text{etc}^4)$$